

6. This exercise is on  $\lambda\rightarrow$ -Curry.

(i) Determine for each of the following terms (if typable) the most general type.

$$\lambda xy.x(yx),$$

**SII**,

**II**.

(ii) Show that the terms  $\lambda xy.yxy$  and  $\mathbf{K}\mathbf{I}(\lambda x.fff)$  are not typable.

7. Investigate for each of the following  $\lambda$ -terms if it is typable in  $\lambda\rightarrow$ . If yes then give a type, if no then explain why not.

$$\lambda xy.x(\mathbf{I}x)y,$$

$$\lambda xy.x(x\mathbf{I})y.$$

8.  $\alpha, \beta$  and  $\gamma$  are different typevariables.

(i) Find inhabitants of

$$(\alpha \rightarrow \beta \rightarrow \gamma) \rightarrow \beta \rightarrow \alpha \rightarrow \gamma$$

$$(\alpha \rightarrow \alpha \rightarrow \beta) \rightarrow \alpha \rightarrow \beta$$

$$(\alpha \rightarrow \alpha \rightarrow \beta) \rightarrow ((\alpha \rightarrow \beta) \rightarrow \gamma) \rightarrow \gamma.$$

(ii) Prove that  $((\alpha \rightarrow \beta) \rightarrow \alpha) \rightarrow \alpha$  is not inhabited. You may use that each typable term has a normal form.

9. In untyped lambda calculus solve

(i)  $Fx = x\mathbf{I}(\mathbf{K}x)$ .

(ii)  $FxF = x\mathbf{I}(Fx)$ .

(iii)  $Fx = x\mathbf{I}(Fx)$ .